

T (28 pts)

Prova 3

2025-01-24

read3Ints : IO (M (Int × Int × Int))

R Escolha 6 dos 10. (6 × 12 pts)

unit, (\*\*) ⊢ pure, ⊗

fmap, join ⊢ (>>=)

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Functor instance para um dos :  $\begin{cases} (\delta \rightarrow) \\ (- \rightarrow \gamma) \end{cases}$

Uma fmap que respeita a lei de (o) mas não de id

sequenceAL : Applicative f ⇒ List (f α) → f (List α)

$$\text{lift} \quad \text{fmap}_f : (\alpha \rightarrow \beta) \rightarrow (f \alpha \rightarrow f \beta)$$

$$\text{ap}_m := (\text{*}_a) \equiv \text{splat}_a : a (\alpha \rightarrow \beta) \rightarrow (a \alpha \rightarrow a \beta)$$

$$\text{bind} \left\{ \begin{array}{l} (\text{=>}_m) : (\alpha \rightarrow m \beta) \rightarrow (m \alpha \rightarrow m \beta) \\ (\text{>=>}_m) : m \alpha \rightarrow (\alpha \rightarrow m \beta) \rightarrow m \beta \end{array} \right.$$

$$\text{join}_m : m (m \alpha) \rightarrow m \alpha$$

$$\text{return}_m := \text{pure}_a : \alpha \rightarrow a \alpha$$

$$\text{kleisli} \left\{ \begin{array}{l} (\text{>=>}_m) : (\alpha \rightarrow m \beta) \rightarrow (\beta \rightarrow m \gamma) \rightarrow (\alpha \rightarrow m \gamma) \\ (\text{=>}_m) : (\beta \rightarrow m \gamma) \rightarrow (\alpha \rightarrow m \beta) \rightarrow (\alpha \rightarrow m \gamma) \end{array} \right.$$

$$(\text{>>}_m) := (\text{*}_a) : a \alpha \rightarrow a \beta \rightarrow a \beta$$

$$\text{void}_f : f \alpha \rightarrow f \mathbb{1}$$

$$\text{unit}_n : n ()$$

$$\text{unit}'_n : \mathbb{1} \rightarrow n ()$$

$$(\text{**})_n : n \alpha \rightarrow n \beta \rightarrow n (\alpha \times \beta) \quad (\text{**}')_n : (n \alpha \times n \beta) \rightarrow n (\alpha \times \beta)$$